

로그인

회원가입

장바구니

전기스쿨소개

교수소개

업데이트 : 2019.03.19



전기스쿨

나의 강의실

커뮤니티

고객센터

인터넷강의

강좌평가

수강신청

강의교재

회원가입 / MEMBER SNS LOGIN



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학생과 학부모, 학생들끼리의 다양한 고민과 리콜 상담해드립니다.

2019 업그레이드 생방송

김대호기술사 1:1 개인교육

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커뮤니티

우리들의 이야기 / 정보공유 / 무료학습자료

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합격수기

무료학습

학습자료

기출문제 자료실

문제복원 자료실

문제복원 QNA

자유게시판



- 글자작게

+ 글자크게

적분공식 총정리 | 학습자료

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작성자 김대호

조회 1 | 추천 0

$$\int \sin ax \, dx = -\frac{\cos ax}{a}$$

$$\int x \sin ax \, dx = \frac{\sin ax}{a^2} - \frac{x \cos ax}{a}$$

$$\int x^2 \sin ax \, dx = \frac{2x}{a^2} \sin ax + \left(\frac{2}{a^3} - \frac{x^2}{a} \right) \cos ax$$

$$\int x^3 \sin ax \, dx = \left(\frac{3x^2}{a^2} - \frac{6}{a^4} \right) \sin ax + \left(\frac{6x}{a^3} - \frac{x^3}{a} \right) \cos ax$$

$$\int \frac{\sin ax}{x} \, dx = ax - \frac{(ax)^3}{3 \cdot 3!} + \frac{(ax)^5}{5 \cdot 5!} - \dots$$

$$\int \frac{\sin ax}{x^2} \, dx = -\frac{\sin ax}{x} + a \int \frac{\cos ax}{x} \, dx \quad [\text{see 14.373}]$$

$$\int \frac{dx}{\sin ax} = \frac{1}{a} \ln (\csc ax - \cot ax) = \frac{1}{a} \ln \tan \frac{ax}{2}$$

$$\int \frac{x \, dx}{\sin ax} = \frac{1}{a^2} \left\{ ax + \frac{(ax)^3}{18} + \frac{7(ax)^5}{1800} + \dots + \frac{2(2^{2n-1} - 1)B_n(ax)^{2n+1}}{(2n+1)!} + \dots \right\}$$

$$\int \sin^2 ax \, dx = \frac{x}{2} - \frac{\sin 2ax}{4a}$$

$$\int x \sin^2 ax \, dx = \frac{x^2}{4} - \frac{x \sin 2ax}{4a} - \frac{\cos 2ax}{8a^2}$$

$$\int \sin^3 ax \, dx = -\frac{\cos ax}{a} + \frac{\cos^3 ax}{3a}$$

$$\int \sin^4 ax \, dx = \frac{3x}{8} - \frac{\sin 2ax}{4a} + \frac{\sin 4ax}{32a}$$

$$\int \frac{dx}{\sin^2 ax} = -\frac{1}{a} \cot ax$$

$$\int \frac{dx}{\sin^3 ax} = -\frac{\cos ax}{2a \sin^2 ax} + \frac{1}{2a} \ln \tan \frac{ax}{2}$$

$$\int \sin px \sin qx \, dx = \frac{\sin (p-q)x}{2(p-q)} - \frac{\sin (p+q)x}{2(p+q)} \quad [\text{If } p = :$$

$$\int \frac{dx}{1 - \sin ax} = \frac{1}{a} \tan \left(\frac{\pi}{4} + \frac{ax}{2} \right)$$

$$\int \frac{x \, dx}{1 - \sin ax} = \frac{x}{a} \tan\left(\frac{\pi}{4} + \frac{ax}{2}\right) + \frac{2}{a^2} \ln \sin\left(\frac{\pi}{4} - \frac{ax}{2}\right)$$

$$\int \frac{dx}{1 + \sin ax} = -\frac{1}{a} \tan\left(\frac{\pi}{4} - \frac{ax}{2}\right)$$

$$\int \frac{x \, dx}{1 + \sin ax} = -\frac{x}{a} \tan\left(\frac{\pi}{4} - \frac{ax}{2}\right) + \frac{2}{a^2} \ln \sin\left(\frac{\pi}{4} + \frac{ax}{2}\right)$$

$$\int \frac{dx}{(1 - \sin ax)^2} = \frac{1}{2a} \tan\left(\frac{\pi}{4} + \frac{ax}{2}\right) + \frac{1}{6a} \tan^3\left(\frac{\pi}{4} + \frac{ax}{2}\right)$$

$$\int \frac{dx}{(1 + \sin ax)^2} = -\frac{1}{2a} \tan\left(\frac{\pi}{4} - \frac{ax}{2}\right) - \frac{1}{6a} \tan^3\left(\frac{\pi}{4} - \frac{ax}{2}\right)$$

$$\int \frac{dx}{p + q \sin ax} = \begin{cases} \frac{2}{a\sqrt{p^2 - q^2}} \tan^{-1} \frac{p \tan \frac{1}{2}ax + q}{\sqrt{p^2 - q^2}} \\ \frac{1}{a\sqrt{q^2 - p^2}} \ln \left(\frac{p \tan \frac{1}{2}ax + q - \sqrt{q^2 - p^2}}{p \tan \frac{1}{2}ax + q + \sqrt{q^2 - p^2}} \right) \end{cases}$$

$$\int \frac{dx}{(p + q \sin ax)^2} = \frac{q \cos ax}{a(p^2 - q^2)(p + q \sin ax)} + \frac{p}{p^2 - q^2} \int \frac{dx}{p + q \sin ax}$$

$$\int \frac{dx}{p^2 + q^2 \sin^2 ax} = \frac{1}{ap\sqrt{p^2 + q^2}} \tan^{-1} \frac{\sqrt{p^2 + q^2} \tan ax}{p}$$

$$\int \frac{dx}{p^2 - q^2 \sin^2 ax} = \begin{cases} \frac{1}{ap\sqrt{p^2 - q^2}} \tan^{-1} \frac{\sqrt{p^2 - q^2} \tan ax}{p} \\ \frac{1}{2ap\sqrt{q^2 - p^2}} \ln \left(\frac{\sqrt{q^2 - p^2} \tan ax + p}{\sqrt{q^2 - p^2} \tan ax - p} \right) \end{cases}$$

$$\int x^m \sin ax \, dx = -\frac{x^m \cos ax}{a} + \frac{mx^{m-1} \sin ax}{a^2} - \frac{m(m-1)}{a^2} \int x^{m-2} \sin ax \, dx$$

$$\int \frac{\sin ax}{x^n} dx = -\frac{\sin ax}{(n-1)x^{n-1}} + \frac{a}{n-1} \int \frac{\cos ax}{x^{n-1}} dx$$

$$\int \sin^n ax \, dx = -\frac{\sin^{n-1} ax \cos ax}{an} + \frac{n-1}{n} \int \sin^{n-2} ax \, dx$$

$$\int \frac{dx}{\sin^n ax} = \frac{-\cos ax}{a(n-1)\sin^{n-1} ax} + \frac{n-2}{n-1} \int \frac{dx}{\sin^{n-2} ax}$$

$$\int \frac{x dx}{\sin^n ax} = \frac{-x \cos ax}{a(n-1)\sin^{n-1} ax} - \frac{1}{a^2(n-1)(n-2)\sin^{n-2} ax} + \frac{n-2}{n-1} \int \frac{x dx}{\sin^{n-2} ax}$$

$$\int \cos ax \, dx = \frac{\sin ax}{a}$$

$$\int x \cos ax \, dx = \frac{\cos ax}{a^2} + \frac{x \sin ax}{a}$$

$$\int x^2 \cos ax \, dx = \frac{2x}{a^2} \cos ax + \left(\frac{x^2}{a} - \frac{2}{a^3} \right) \sin ax$$

$$\int x^3 \cos ax \, dx = \left(\frac{3x^2}{a^2} - \frac{6}{a^4} \right) \cos ax + \left(\frac{x^3}{a} - \frac{6x}{a^3} \right) \sin ax$$

$$\int \frac{\cos ax}{x} \, dx = \ln x - \frac{(ax)^2}{2 \cdot 2!} + \frac{(ax)^4}{4 \cdot 4!} - \frac{(ax)^6}{6 \cdot 6!} + \dots$$

$$\int \frac{\cos ax}{x^2} \, dx = -\frac{\cos ax}{x} - a \int \frac{\sin ax}{x} \, dx \quad [\text{See 14.343}]$$

$$\int \frac{dx}{\cos ax} = \frac{1}{a} \ln (\sec ax + \tan ax) = \frac{1}{a} \ln \tan \left(\frac{\pi}{4} + \frac{ax}{2} \right)$$

$$\int \frac{x dx}{\cos ax} = \frac{1}{a^2} \left\{ \frac{(ax)^2}{2} + \frac{(ax)^4}{8} + \frac{5(ax)^6}{144} + \dots + \frac{E_n(ax)^{2n+2}}{(2n+2)(2n)!} + \dots \right\}$$

$$\int \cos^2 ax \, dx = \frac{x}{2} + \frac{\sin 2ax}{4a}$$

$$\int x \cos^2 ax \, dx = \frac{x^2}{4} + \frac{x \sin 2ax}{4a} + \frac{\cos 2ax}{8a^2}$$

$$\int \cos^3 ax \, dx = \frac{\sin ax}{a} - \frac{\sin^3 ax}{3a}$$

$$\int \cos^4 ax \, dx = \frac{3x}{8} + \frac{\sin 2ax}{4a} + \frac{\sin 4ax}{32a}$$

$$\int \frac{dx}{\cos^2 ax} = \frac{\tan ax}{a}$$

$$\int \frac{dx}{\cos^3 ax} = \frac{\sin ax}{2a \cos^2 ax} + \frac{1}{2a} \ln \tan \left(\frac{\pi}{4} + \frac{ax}{2} \right)$$

$$\int \cos ax \cos px \, dx = \frac{\sin (a-p)x}{2(a-p)} + \frac{\sin (a+p)x}{2(a+p)}$$

$$\int \frac{dx}{1 - \cos ax} = -\frac{1}{a} \cot \frac{ax}{2}$$

$$\int \frac{x \, dx}{1 - \cos ax} = -\frac{x}{a} \cot \frac{ax}{2} + \frac{2}{a^2} \ln \sin \frac{ax}{2}$$

$$\int \frac{dx}{1 + \cos ax} = \frac{1}{a} \tan \frac{ax}{2}$$

$$\int \frac{x \, dx}{1 + \cos ax} = \frac{x}{a} \tan \frac{ax}{2} + \frac{2}{a^2} \ln \cos \frac{ax}{2}$$

$$\int \frac{dx}{(1 - \cos ax)^2} = -\frac{1}{2a} \cot \frac{ax}{2} - \frac{1}{6a} \cot^3 \frac{ax}{2}$$

$$\int \frac{dx}{(1 + \cos ax)^2} = \frac{1}{2a} \tan \frac{ax}{2} + \frac{1}{6a} \tan^3 \frac{ax}{2}$$

$$\int x^m \cos ax \, dx = \frac{x^m \sin ax}{a} + \frac{mx^{m-1}}{a^2} \cos ax - \frac{m(m-1)}{a^2} \int x^{m-2} \cos ax \, dx$$

$$\int \frac{\cos ax}{x^n} \, dx = -\frac{\cos ax}{(n-1)x^{n-1}} - \frac{a}{n-1} \int \frac{\sin ax}{x^{n-1}} \, dx$$

$$\int \cos^n ax \, dx = \frac{\sin ax \cos^{n-1} ax}{an} + \frac{n-1}{n} \int \cos^{n-2} ax \, dx$$

$$\int \frac{dx}{\cos^n ax} = \frac{\sin ax}{a(n-1) \cos^{n-1} ax} + \frac{n-2}{n-1} \int \frac{dx}{\cos^{n-2} ax}$$

$$\int \frac{x \, dx}{\cos^n ax} = \frac{x \sin ax}{a(n-1) \cos^{n-1} ax} - \frac{1}{a^2(n-1)(n-2) \cos^{n-2} ax} + \frac{n-2}{n-1} \int \frac{x \, dx}{\cos^{n-2} ax}$$

$$\int \sin ax \cos ax \, dx = \frac{\sin^2 ax}{2a}$$

$$\int \sin px \cos qx \, dx = -\frac{\cos (p-q)x}{2(p-q)} - \frac{\cos (p+q)x}{2(p+q)}$$

$$\int \sin^n ax \cos ax \, dx = \frac{\sin^{n+1} ax}{(n+1)a}$$

$$\int \cos^n ax \sin ax \, dx = -\frac{\cos^{n+1} ax}{(n+1)a}$$

$$\int \sin^2 ax \cos^2 ax \, dx = \frac{x}{8} - \frac{\sin 4ax}{32a}$$

$$\int \frac{dx}{\sin ax \cos ax} = \frac{1}{a} \ln \tan ax$$

$$\int \frac{dx}{\sin^2 ax \cos ax} = \frac{1}{a} \ln \tan \left(\frac{\pi}{4} + \frac{ax}{2} \right) - \frac{1}{a \sin ax}$$

$$\int \frac{dx}{\sin ax \cos^2 ax} = \frac{1}{a} \ln \tan \frac{ax}{2} + \frac{1}{a \cos ax}$$

$$\int \frac{dx}{\sin^2 ax \cos^2 ax} = -\frac{2 \cot 2ax}{a}$$

$$\int \frac{\sin^2 ax}{\cos ax} \, dx = -\frac{\sin ax}{a} + \frac{1}{a} \ln \tan \left(\frac{ax}{2} + \frac{\pi}{4} \right)$$

$$\int \frac{\cos^2 ax}{\sin ax} \, dx = \frac{\cos ax}{a} + \frac{1}{a} \ln \tan \frac{ax}{2}$$

$$\int \frac{dx}{\cos ax(1 \pm \sin ax)} = \mp \frac{1}{2a(1 \pm \sin ax)} + \frac{1}{2a} \ln \tan \left(\frac{ax}{2} + \frac{\pi}{4} \right)$$

$$\int \frac{dx}{\sin ax(1 \pm \cos ax)} = \pm \frac{1}{2a(1 \pm \cos ax)} + \frac{1}{2a} \ln \tan \frac{ax}{2}$$

$$\int \frac{dx}{\sin ax \pm \cos ax} = \frac{1}{a\sqrt{2}} \ln \tan \left(\frac{ax}{2} \pm \frac{\pi}{8} \right)$$

$$\int \frac{\sin ax \, dx}{\sin ax \pm \cos ax} = \frac{x}{2} \mp \frac{1}{2a} \ln (\sin ax \pm \cos ax)$$

$$\int \frac{\cos ax \, dx}{\sin ax \pm \cos ax} = \pm \frac{x}{2} + \frac{1}{2a} \ln(\sin ax \pm \cos ax)$$

$$\int \frac{\sin ax \, dx}{p + q \cos ax} = -\frac{1}{aq} \ln(p + q \cos ax)$$

$$\int \frac{\cos ax \, dx}{p + q \sin ax} = \frac{1}{aq} \ln(p + q \sin ax)$$

$$\int \frac{\sin ax \, dx}{(p + q \cos ax)^n} = \frac{1}{aq(n-1)(p + q \cos ax)^{n-1}}$$

$$\int \frac{\cos ax \, dx}{(p + q \sin ax)^n} = \frac{1}{aq(n-1)(p + q \sin ax)^{n-1}}$$

$$\int \frac{dx}{p \sin ax + q \cos ax} = \frac{1}{a\sqrt{p^2 + q^2}} \ln \tan \left(\frac{ax + \tan^{-1}(q/p)}{2} \right)$$

$$\int \sin^m ax \cos^n ax \, dx = \begin{cases} -\frac{\sin^{m-1} ax \cos^{n+1} ax}{a(m+n)} + \frac{m-1}{m+n} \int \sin^{m-2} ax \cos^n ax \, dx \\ \frac{\sin^{m+1} ax \cos^{n-1} ax}{a(m+n)} + \frac{n-1}{m+n} \int \sin^m ax \cos^{n-2} ax \, dx \end{cases}$$

$$\int \frac{\sin^m ax}{\cos^n ax} \, dx = \begin{cases} \frac{\sin^{m-1} ax}{a(n-1) \cos^{n-1} ax} - \frac{m-1}{n-1} \int \frac{\sin^{m-2} ax}{\cos^{n-2} ax} \, dx \\ \frac{\sin^{m+1} ax}{a(n-1) \cos^{n-1} ax} - \frac{m-n+2}{n-1} \int \frac{\sin^m ax}{\cos^{n-2} ax} \, dx \\ \frac{-\sin^{m-1} ax}{a(m-n) \cos^{n-1} ax} + \frac{m-1}{m-n} \int \frac{\sin^{m-2} ax}{\cos^n ax} \, dx \end{cases}$$

$$\int \frac{\cos^m ax}{\sin^n ax} \, dx = \begin{cases} \frac{-\cos^{m-1} ax}{a(n-1) \sin^{n-1} ax} - \frac{m-1}{n-1} \int \frac{\cos^{m-2} ax}{\sin^{n-2} ax} \, dx \\ \frac{-\cos^{m+1} ax}{a(n-1) \sin^{n-1} ax} - \frac{m-n+2}{n-1} \int \frac{\cos^m ax}{\sin^{n-2} ax} \, dx \\ \frac{\cos^{m-1} ax}{a(m-n) \sin^{n-1} ax} + \frac{m-1}{m-n} \int \frac{\cos^{m-2} ax}{\sin^n ax} \, dx \end{cases}$$

$$\int \frac{dx}{\sin^m ax \cos^n ax} = \begin{cases} \frac{1}{a(n-1) \sin^{m-1} ax \cos^{n-1} ax} + \frac{m+n-2}{n-1} \int \frac{dx}{\sin^m ax \cos^{n-2} ax} \\ \frac{-1}{a(m-1) \sin^{m-1} ax \cos^{n-1} ax} + \frac{m+n-2}{m-1} \int \frac{dx}{\sin^{m-2} ax \cos^n ax} \end{cases}$$

$$\int \tan ax \, dx = -\frac{1}{a} \ln \cos ax = \frac{1}{a} \ln \sec ax$$

$$\int \tan^2 ax \, dx = \frac{\tan ax}{a} - x$$

$$\int \tan^3 ax \, dx = \frac{\tan^2 ax}{2a} + \frac{1}{a} \ln \cos ax$$

$$\int \tan^n ax \sec^2 ax \, dx = \frac{\tan^{n+1} ax}{(n+1)a}$$

$$\int \frac{\sec^2 ax}{\tan ax} \, dx = \frac{1}{a} \ln \tan ax$$

$$\int \frac{dx}{\tan ax} = \frac{1}{a} \ln \sin ax$$

$$\int x \tan ax \, dx = \frac{1}{a^2} \left\{ \frac{(ax)^3}{3} + \frac{(ax)^5}{15} + \frac{2(ax)^7}{105} + \dots + \frac{2^{2n}(2^{2n}-1)B_n(ax)^{2n+1}}{(2n+1)!} + \dots \right\}$$

$$\int \frac{\tan ax}{x} \, dx = ax + \frac{(ax)^3}{9} + \frac{2(ax)^5}{75} + \dots + \frac{2^{2n}(2^{2n}-1)B_n(ax)^{2n-1}}{(2n-1)(2n)!} + \dots$$

$$\int x \tan^2 ax \, dx = \frac{x \tan ax}{a} + \frac{1}{a^2} \ln \cos ax - \frac{x^2}{2}$$

$$\int \frac{dx}{p + q \tan ax} = \frac{px}{p^2 + q^2} + \frac{q}{a(p^2 + q^2)} \ln (q \sin ax + p \cos ax)$$

$$\int \frac{dx}{p + q \cot ax} = \frac{px}{p^2 + q^2} - \frac{q}{a(p^2 + q^2)} \ln(p \sin ax + q \cos ax)$$

$$\int \cot^n ax \, dx = -\frac{\cot^{n-1} ax}{(n-1)a} - \int \cot^{n-2} ax \, dx$$

$$\int \sec ax \, dx = \frac{1}{a} \ln(\sec ax + \tan ax) = \frac{1}{a} \ln \tan \left(\frac{ax}{2} + \frac{\pi}{4} \right)$$

$$\int \sec^2 ax \, dx = \frac{\tan ax}{a}$$

$$\int \sec^3 ax \, dx = \frac{\sec ax \tan ax}{2a} + \frac{1}{2a} \ln(\sec ax + \tan ax)$$

$$\int \sec^n ax \tan ax \, dx = \frac{\sec^n ax}{na}$$

$$\int \frac{dx}{\sec ax} = \frac{\sin ax}{a}$$

$$\int x \sec ax \, dx = \frac{1}{a^2} \left\{ \frac{(ax)^2}{2} + \frac{(ax)^4}{8} + \frac{5(ax)^6}{144} + \dots + \frac{E_n(ax)^{2n+2}}{(2n+2)(2n)!} + \dots \right\}$$

$$\int \frac{\sec ax}{x} \, dx = \ln x + \frac{(ax)^2}{4} + \frac{5(ax)^4}{96} + \frac{61(ax)^6}{4320} + \dots + \frac{E_n(ax)^{2n}}{2n(2n)!} + \dots$$

$$\int x \sec^2 ax \, dx = \frac{x}{a} \tan ax + \frac{1}{a^2} \ln \cos ax$$

$$\int \frac{dx}{q + p \sec ax} = \frac{x}{q} - \frac{p}{q} \int \frac{dx}{p + q \cos ax}$$

$$\int \sec^n ax \, dx = \frac{\sec^{n-2} ax \tan ax}{a(n-1)} + \frac{n-2}{n-1} \int \sec^{n-2} ax \, dx$$

$$\int \csc ax \, dx = \frac{1}{a} \ln(\csc ax - \cot ax) = \frac{1}{a} \ln \tan \frac{ax}{2}$$

$$\int \csc^2 ax \, dx = -\frac{\cot ax}{a}$$

$$\int \csc^3 ax \, dx = -\frac{\csc ax \cot ax}{2a} + \frac{1}{2a} \ln \tan \frac{ax}{2}$$

$$\int \csc^n ax \cot ax \, dx = -\frac{\csc^n ax}{na}$$

$$\int \frac{dx}{\csc ax} = -\frac{\cos ax}{a}$$

$$\int x \csc ax \, dx = \frac{1}{a^2} \left\{ ax + \frac{(ax)^3}{18} + \frac{7(ax)^5}{1800} + \dots + \frac{2(2^{2n-1}-1)B_n(ax)^{2n+1}}{(2n+1)!} + \dots \right\}$$

$$\int \frac{\csc ax}{x} \, dx = -\frac{1}{ax} + \frac{ax}{6} + \frac{7(ax)^3}{1080} + \dots + \frac{2(2^{2n-1}-1)B_n(ax)^{2n-1}}{(2n-1)(2n)!} + \dots$$

$$\int x \csc^2 ax \, dx = -\frac{x \cot ax}{a} + \frac{1}{a^2} \ln \sin ax$$

$$\int \frac{dx}{q + p \csc ax} = \frac{x}{q} - \frac{p}{q} \int \frac{dx}{p + q \sin ax}$$

$$\int \csc^n ax \, dx = -\frac{\csc^{n-2} ax \cot ax}{a(n-1)} + \frac{n-2}{n-1} \int \csc^{n-2} ax \, dx$$

$$\int \sin^{-1} \frac{x}{a} dx = x \sin^{-1} \frac{x}{a} + \sqrt{a^2 - x^2}$$

$$\int x \sin^{-1} \frac{x}{a} dx = \left(\frac{x^2}{2} - \frac{a^2}{4} \right) \sin^{-1} \frac{x}{a} + \frac{x\sqrt{a^2 - x^2}}{4}$$

$$\int x^2 \sin^{-1} \frac{x}{a} dx = \frac{x^3}{3} \sin^{-1} \frac{x}{a} + \frac{(x^2 + 2a^2)\sqrt{a^2 - x^2}}{9}$$

$$\int \frac{\sin^{-1}(x/a)}{x} dx = \frac{x}{a} + \frac{(x/a)^3}{2 \cdot 3 \cdot 3} + \frac{1 \cdot 3(x/a)^5}{2 \cdot 4 \cdot 5 \cdot 5} + \frac{1 \cdot 3 \cdot 5(x/a)^7}{2 \cdot 4 \cdot 6 \cdot 7 \cdot 7} + \dots$$

$$\int \frac{\sin^{-1}(x/a)}{x^2} dx = -\frac{\sin^{-1}(x/a)}{x} - \frac{1}{a} \ln \left(\frac{a + \sqrt{a^2 - x^2}}{x} \right)$$

$$\int \left(\sin^{-1} \frac{x}{a} \right)^2 dx = x \left(\sin^{-1} \frac{x}{a} \right)^2 - 2x + 2\sqrt{a^2 - x^2} \sin^{-1} \frac{x}{a}$$

$$\int \cos^{-1} \frac{x}{a} dx = x \cos^{-1} \frac{x}{a} - \sqrt{a^2 - x^2}$$

$$\int x \cos^{-1} \frac{x}{a} dx = \left(\frac{x^2}{2} - \frac{a^2}{4} \right) \cos^{-1} \frac{x}{a} - \frac{x\sqrt{a^2 - x^2}}{4}$$

$$\int x^2 \cos^{-1} \frac{x}{a} dx = \frac{x^3}{3} \cos^{-1} \frac{x}{a} - \frac{(x^2 + 2a^2)\sqrt{a^2 - x^2}}{9}$$

$$\int \frac{\cos^{-1}(x/a)}{x} dx = \frac{\pi}{2} \ln x - \int \frac{\sin^{-1}(x/a)}{x} dx$$

$$\int \frac{\cos^{-1}(x/a)}{x^2} dx = -\frac{\cos^{-1}(x/a)}{x} + \frac{1}{a} \ln \left(\frac{a + \sqrt{a^2 - x^2}}{x} \right)$$

$$\int \left(\cos^{-1} \frac{x}{a} \right)^2 dx = x \left(\cos^{-1} \frac{x}{a} \right)^2 - 2x - 2\sqrt{a^2 - x^2} \cos^{-1} \frac{x}{a}$$

$$\int \tan^{-1} \frac{x}{a} dx = x \tan^{-1} \frac{x}{a} - \frac{a}{2} \ln(x^2 + a^2)$$

$$\int x \tan^{-1} \frac{x}{a} dx = \frac{1}{2}(x^2 + a^2) \tan^{-1} \frac{x}{a} - \frac{ax}{2}$$

$$\int x^2 \tan^{-1} \frac{x}{a} dx = \frac{x^3}{3} \tan^{-1} \frac{x}{a} - \frac{ax^2}{6} + \frac{a^3}{6} \ln(x^2 + a^2)$$

$$\int \frac{\tan^{-1}(x/a)}{x} dx = \frac{x}{a} - \frac{(x/a)^3}{3^2} + \frac{(x/a)^5}{5^2} - \frac{(x/a)^7}{7^2} + \dots$$

$$\int \frac{\tan^{-1}(x/a)}{x^2} dx = -\frac{1}{x} \tan^{-1} \frac{x}{a} - \frac{1}{2a} \ln \left(\frac{x^2 + a^2}{x^2} \right)$$

$$\int \cot^{-1} \frac{x}{a} dx = x \cot^{-1} \frac{x}{a} + \frac{a}{2} \ln(x^2 + a^2)$$

$$\int x \cot^{-1} \frac{x}{a} dx = \frac{1}{2}(x^2 + a^2) \cot^{-1} \frac{x}{a} + \frac{ax}{2}$$

$$\int x^m \sin^{-1} \frac{x}{a} dx = \frac{x^{m+1}}{m+1} \sin^{-1} \frac{x}{a} - \frac{1}{m+1} \int \frac{x^{m+1}}{\sqrt{a^2 - x^2}} dx$$

$$\int x^m \cos^{-1} \frac{x}{a} dx = \frac{x^{m+1}}{m+1} \cos^{-1} \frac{x}{a} + \frac{1}{m+1} \int \frac{x^{m+1}}{\sqrt{a^2 - x^2}} dx$$

$$\int x^m \tan^{-1} \frac{x}{a} dx = \frac{x^{m+1}}{m+1} \tan^{-1} \frac{x}{a} - \frac{a}{m+1} \int \frac{x^{m+1}}{x^2 + a^2} dx$$

$$\int x^m \cot^{-1} \frac{x}{a} dx = \frac{x^{m+1}}{m+1} \cot^{-1} \frac{x}{a} + \frac{a}{m+1} \int \frac{x^{m+1}}{x^2 + a^2} dx$$

$$\int e^{ax} dx = \frac{e^{ax}}{a}$$

$$\int x e^{ax} dx = \frac{e^{ax}}{a} \left(x - \frac{1}{a} \right)$$

$$\int x^2 e^{ax} dx = \frac{e^{ax}}{a} \left(x^2 - \frac{2x}{a} + \frac{2}{a^2} \right)$$

$$\begin{aligned}\int x^n e^{ax} dx &= \frac{x^n e^{ax}}{a} - \frac{n}{a} \int x^{n-1} e^{ax} dx \\ &= \frac{e^{ax}}{a} \left(x^n - \frac{nx^{n-1}}{a} + \frac{n(n-1)x^{n-2}}{a^2} - \dots - \frac{(-1)^n n!}{a^n} \right)\end{aligned}$$

$$\int \frac{e^{ax}}{x} dx = \ln x + \frac{ax}{1 \cdot 1!} + \frac{(ax)^2}{2 \cdot 2!} + \frac{(ax)^3}{3 \cdot 3!} + \dots$$

$$\int \frac{e^{ax}}{x^n} dx = \frac{-e^{ax}}{(n-1)x^{n-1}} + \frac{a}{n-1} \int \frac{e^{ax}}{x^{n-1}} dx$$

$$\int \frac{dx}{p + qe^{ax}} = \frac{x}{p} - \frac{1}{ap} \ln(p + qe^{ax})$$

$$\int \frac{dx}{(p + qe^{ax})^2} = \frac{x}{p^2} + \frac{1}{ap(p + qe^{ax})} - \frac{1}{ap^2} \ln(p + qe^{ax})$$

$$\int \frac{dx}{pe^{ax} + qe^{-ax}} = \begin{cases} \frac{1}{a\sqrt{pq}} \tan^{-1} \left(\sqrt{\frac{p}{q}} e^{ax} \right) \\ \frac{1}{2a\sqrt{-pq}} \ln \left(\frac{e^{ax} - \sqrt{-q/p}}{e^{ax} + \sqrt{-q/p}} \right) \end{cases}$$

$$\int e^{ax} \sin bx dx = \frac{e^{ax}(a \sin bx - b \cos bx)}{a^2 + b^2}$$

$$\int e^{ax} \cos bx dx = \frac{e^{ax}(a \cos bx + b \sin bx)}{a^2 + b^2}$$

$$\int xe^{ax} \sin bx dx = \frac{xe^{ax}(a \sin bx - b \cos bx)}{a^2 + b^2} - \frac{e^{ax}\{(a^2 - b^2) \sin bx - 2ab \cos bx\}}{(a^2 + b^2)^2}$$

$$\int xe^{ax} \cos bx dx = \frac{xe^{ax}(a \cos bx + b \sin bx)}{a^2 + b^2} - \frac{e^{ax}\{(a^2 - b^2) \cos bx + 2ab \sin bx\}}{(a^2 + b^2)^2}$$

$$\int e^{ax} \ln x dx = \frac{e^{ax} \ln x}{a} - \frac{1}{a} \int \frac{e^{ax}}{x} dx$$

$$\int e^{ax} \sin^n bx \, dx = \frac{e^{ax} \sin^{n-1} bx}{a^2 + n^2 b^2} (a \sin bx - nb \cos bx) + \frac{n(n-1)b^2}{a^2 + n^2 b^2} \int e^{ax} \sin^{n-2} bx \, dx$$

$$\int e^{ax} \cos^n bx \, dx = \frac{e^{ax} \cos^{n-1} bx}{a^2 + n^2 b^2} (a \cos bx + nb \sin bx) + \frac{n(n-1)b^2}{a^2 + n^2 b^2} \int e^{ax} \cos^{n-2} bx \, dx$$

$$\int \ln x \, dx = x \ln x - x$$

$$\int x \ln x \, dx = \frac{x^2}{2} (\ln x - \frac{1}{2})$$

$$\int x^m \ln x \, dx = \frac{x^{m+1}}{m+1} \left(\ln x - \frac{1}{m+1} \right)$$

$$\int \frac{\ln x}{x} \, dx = \frac{1}{2} \ln^2 x$$

$$\int \frac{\ln x}{x^2} \, dx = -\frac{\ln x}{x} - \frac{1}{x}$$

$$\int \ln^2 x \, dx = x \ln^2 x - 2x \ln x + 2x$$

$$\int \frac{\ln^n x \, dx}{x} = \frac{\ln^{n+1} x}{n+1}$$

$$\int \frac{dx}{x \ln x} = \ln(\ln x)$$

$$\int \frac{dx}{\ln x} = \ln(\ln x) + \ln x + \frac{\ln^2 x}{2 \cdot 2!} + \frac{\ln^3 x}{3 \cdot 3!} + \dots$$

$$\int \frac{x^m dx}{\ln x} = \ln(\ln x) + (m+1) \ln x + \frac{(m+1)^2 \ln^2 x}{2 \cdot 2!} + \frac{(m+1)^3 \ln^3 x}{3 \cdot 3!} + \dots$$

$$\int \ln^n x \, dx = x \ln^n x - n \int \ln^{n-1} x \, dx$$






$$\int x^m \ln^n x \, dx = \frac{x^{m+1} \ln^n x}{m+1} - \frac{n}{m+1} \int x^m \ln^{n-1} x \, dx$$

$$\int \ln(x^2 + a^2) \, dx = x \ln(x^2 + a^2) - 2x + 2a \tan^{-1} \frac{x}{a}$$

$$\int \ln(x^2 - a^2) \, dx = x \ln(x^2 - a^2) - 2x + a \ln \left(\frac{x+a}{x-a} \right)$$

$$\int x^m \ln(x^2 \pm a^2) \, dx = \frac{x^{m+1} \ln(x^2 \pm a^2)}{m+1} - \frac{2}{m+1} \int \frac{x^{m+2}}{x^2 \pm a^2} \, dx$$

댓글쓰기

번호	제목	등록인	등록일	추천수	조회수	비고
833	[기사필기] 적분공식 총정리  (0)	김대호	2019-03-19	0	1	
832	[기사실기] NVS  (0)	김대호	2019-03-11	0	59	
831	[기사실기] 접지극 불이 콘센트와 접지단자 불이 콘센트  (0)	김대호	2019-03-09	0	60	